

# A Comparison of Strain Deformation Mechanism of Al, Mo, MgO & CaO in Harper-Dorn Creep

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## ABSTRACT

Harper-Dorn creep Mechanism is studied for Al, Mo, MgO and CaO. The normalized grain size for each material is compared by using Langdon-Mohamed Type deformation mechanism maps [7]. Al is an F.C.C. metal, Mo is a B.C.C. metal, whereas CaO and MgO are non-metallic oxides, they all have different physical properties and hence this case study has a wide range of spectrum.

Key Terms: Harper-Dorn Creep, Creep deformation mechanism, Creep deformation maps.

## 1. INTRODUCTION

A new mechanism was developed for Harper-Dorn creep[3], in which the creep rate  $\varepsilon_{HD}$  is given by

$$\varepsilon_{HD} = A_{HD} \left[ \frac{D_1 G b}{kT} \right] \left( \frac{\sigma}{G} \right) \quad (1)$$

Where:  $D_1$  is the diffusion co-efficient,  $G$  is the shear modulus,  $b$  is the Burger's vector,  $k$  is Boltzmann's constant,  $T$  is absolute temperature,  $\sigma$  is the normal stress and  $A_{HD}$  is a constant given by

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$$A_{HD} = \frac{1.4\pi\left(\frac{\tau_p}{G}\right)^2}{-\ln\left(\frac{\tau_p}{G}\right)} \quad (2)$$

Where  $\tau_p$  is the Peierl's stress,

Since the magnitude of  $\tau_p$  varies significantly between materials with different crystallographic structures, the effect of structure was investigated by constructing maps [4,5,&7] for Al (typical f.c.c metal), Mo (typical b.c.c. metal), CaO and MgO (typical non-metallic oxides) [2]. The values of  $\tau_p / G$ ,  $T_m$  and  $A_{HD}$  for different materials are given in Table 1, [3].

Maps were constructed by using the relationships for Nabarro-Herring creep, power law creep at high temperature, and Harper-Dorn creep (figures 1-5). The relationships for Coble creep and power law at low temperature were not included in the analysis. The values of  $A_1$  and 'n' for each material are given in Table 2.

## 2. DEFORMATION MECHANISMS

The dominant deformation mechanisms occurring at high temperature creep are briefly described as below:

### **Dislocation Glide**

A dislocation moves across a slip plane thereby deforming the crystal by deforming glide. This deformation is observed at stress level below the strength and where there no effects from diffusion.

### **Dislocation Climb**

A pure edge dislocation can move in a direction perpendicular to its length. However it may move perpendicular to the glide plane, by a process known as climb.



Climb (H.T) 
$$\varepsilon_c = A_1 D_{o(1)} e^{-Q_1/RT} (Gb/kT)(\sigma/G)^n \quad (7)$$

Equations (3) and (5) give values of (d/b) which separates Harper-Dorn and Nabarro-Herring by horizontal line:

$$d/b = (28A_{HD})^{1/2} \quad (8)$$

Equations (5) and (7) give values of  $\sigma/G$  which which separates Harper-Dorn and Power law creep (H. T.)

$$\sigma/G = (A_{HD}/A_1)^{\frac{1}{n+1}} \quad (9)$$

On double logarithmic plot the slope of the line separating Nabarro-Herring and Power law creep is calculated by equation (10)

$$Slope = \frac{1-n}{2} \quad (10)$$

The values of (d/b),  $\sigma/G$  and slopes calculated for each material are listed in Table 3.

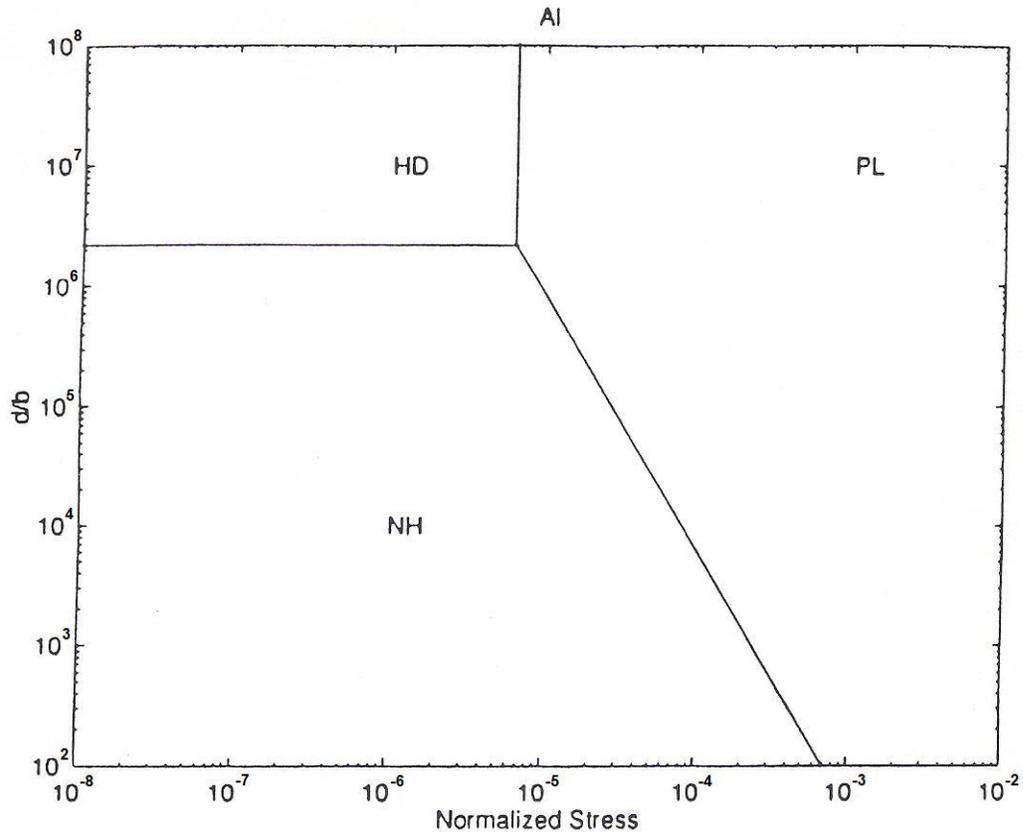


Figure 1: Harper-Dorn creep for Aluminum

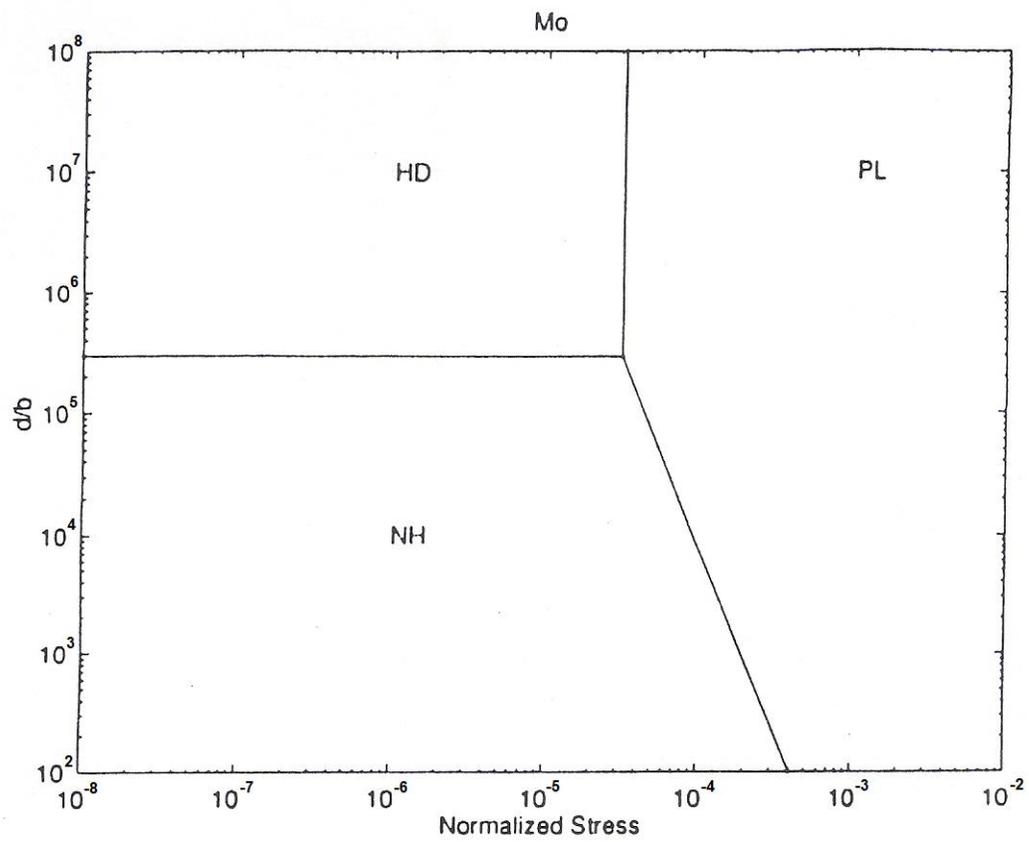


Figure 2: Harper-Dorn creep for Mo

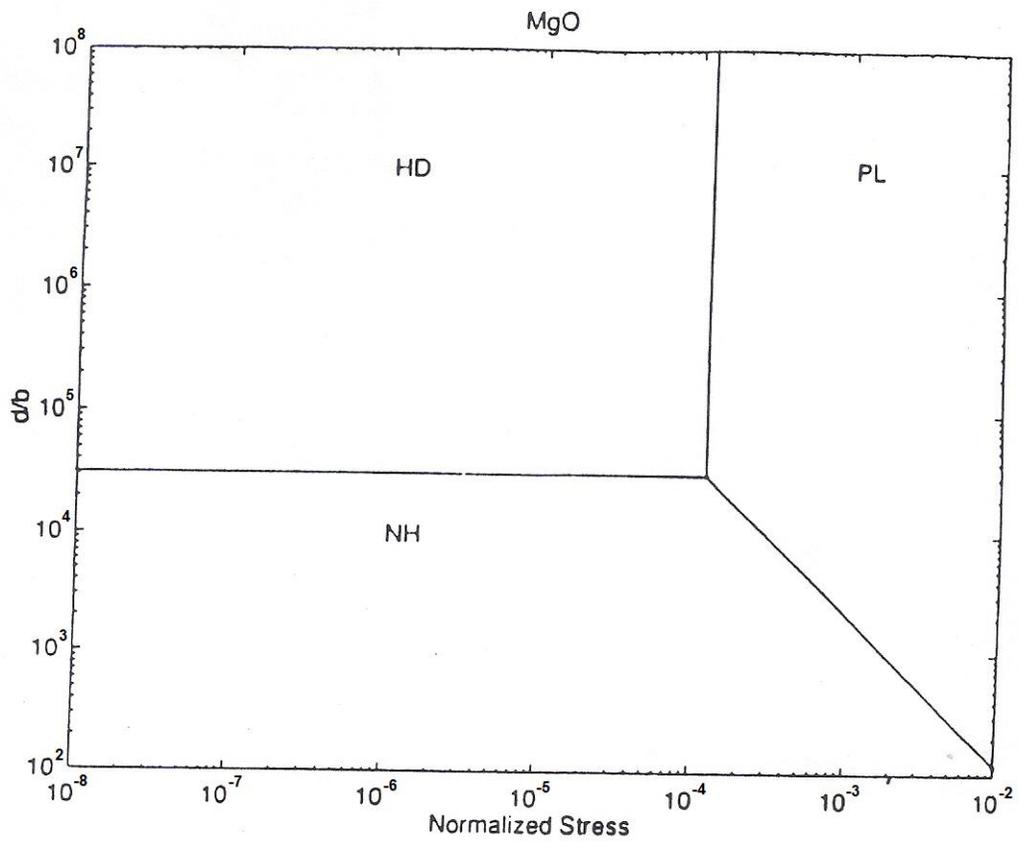


Figure 3: Harper-Doorn creep for MgO

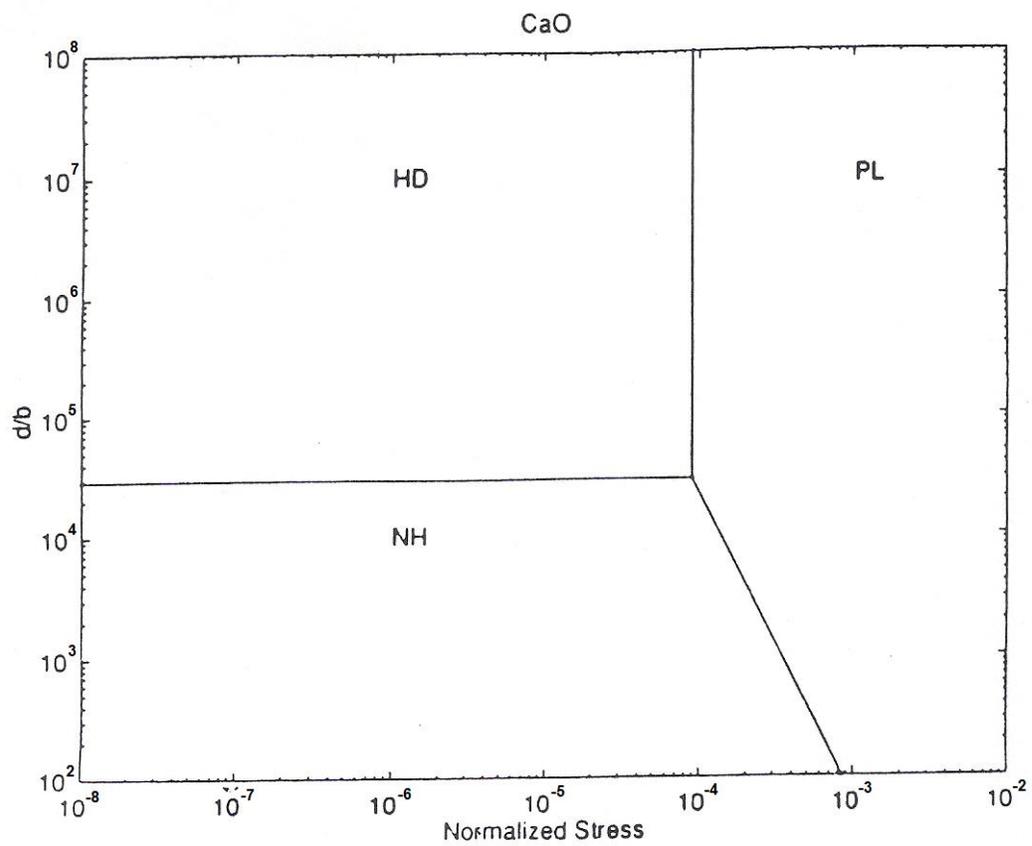


Figure 4: Harper-Dorn creep for CaO

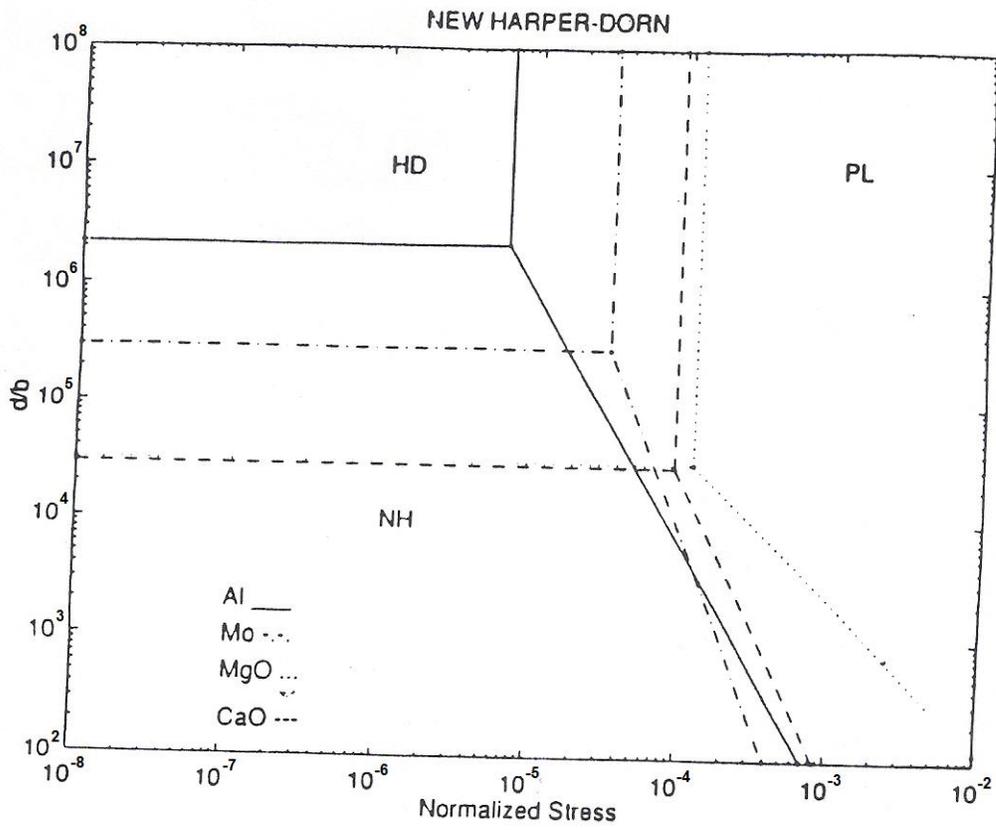


Figure 5: A comparison of Al, Mo, MgO, and CaO in Harper-Dorn creep.

Table 1: The values of  $\tau_p/G$ , Temperature and  $A_{HD}$  for different materials

Material	$\tau_p/G$	Temperature	$A_{HD}$
Al	$4 \times 10^{-6}$	$0.98 T_m$	$5.66 \times 10^{-12}$
Mo	$2.77 \times 10^{-5}$	$0.91 T_m$	$3.21 \times 10^{-10}$
CaO	$2.5 \times 10^{-4}$	$0.54 T_m$	$3.31 \times 10^{-8}$
MgO	$2.33 \times 10^{-4}$	$0.63 T_m$	$2.85 \times 10^{-8}$

Table 2: The values of different parameters for Harper\_Dorn creep

Material	Class	$A_{HD}$	$A_1$	n
Al	F. C. C.	$5.66 \times 10^{-12}$	$2.5 \times 10^6$	4.4
Mo	B. C. C.	$3.21 \times 10^{-10}$	$1 \times 10^{13}$	6.0
CaO	Ceramic	$3.31 \times 10^{-8}$	$5 \times 10^6$	5.0
MgO	Ceramic	$2.855 \times 10^{-8}$	2.0	3.0

Table 3: The values of (d/b),  $\sigma/G$  and slopes for Harper-Dorn creep

Material	d/b	$\sigma/G$	slope
Al	$2.2 \times 10^6$	$6.45 \times 10^{-6}$	-1.7
Mo	$2.95 \times 10^5$	$3.2 \times 10^{-5}$	-2.5
MgO	$3.12 \times 10^4$	$1.2 \times 10^{-4}$	-1.0
CaO	$2.91 \times 10^4$	$9.0 \times 10^{-6}$	-2.0

## 4. CONCLUSION

A comparison of Harper-Dorn creep shows that the value of normalized grain size for materials for b.c.c. materials (e.g. Mo) and non-metallic oxides (e.g. MgO and CaO) is smaller than f.c.c. metals (e.g. Al) under the same conditions of stress and temperature.

## 5. ACKNOWLEDGEMENT

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## 6. NOMENCLATURE

$T_m$	melting temperature	$b$	Burger's vector
$A_1$	constant	$k$	Boltzmann's constant
$N$	index	$\sigma$	normal stress
$D_1$	diffusion co-efficient	B.C.C.	body centered cube
$G$	shear modulus	F.C.C.	faced centered cube

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